

P. 303 #1-9 ANSWERS

1. Natural - always exist naturally occurring, i.e. - planet
Artificial - manmade, put into orbit by humans - satellites.
2. Microgravity - the environment present when an object is in freefall
3. GPS Satellites - rely on position triangulation.
- 4a) Orbit at the same rate as Earth
b) Appears in the sky at the same time each day
c) In the same spot all of the time.
5. For a geosynchronous orbit the time is $24 \text{ hr} = 86400 \text{ s}$.

$$v = \sqrt{\frac{Gm}{r}} \Rightarrow v^2 = \frac{Gm}{r}$$

$$\text{But } v = \frac{d}{t} = \frac{2\pi r}{t}$$

$$\therefore \left(\frac{2\pi r}{t}\right)^2 = \frac{Gm}{r}$$

$$\frac{4\pi^2 r^2}{t^2} = \frac{Gm}{r}$$

$$r^3 = \frac{Gm t^2}{4\pi^2}$$

$$r = \left(\frac{Gm t^2}{4\pi^2}\right)^{1/3}$$

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$$r = \left(\frac{(6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2) (5.98 \times 10^{24} \text{ kg}) (86400 \text{ s})^2}{4\pi^2} \right)^{1/3}$$

$$r = 4.2 \times 10^7 \text{ m}$$

6 a) $r = 4.5 \times 10^9 \text{ km}$
 $= 4.5 \times 10^{12} \text{ m}$

$T = 164.5 \text{ Earth years}$
 $= 164.5 (365.25) (24) (60) (60)$
 $= 5.191 \times 10^9 \text{ s}$

$v = ?$

$$v = \frac{d}{t}$$

$$v = \frac{2\pi r}{T}$$

$$= \frac{2\pi (4.5 \times 10^{12} \text{ m})}{5.191 \times 10^9 \text{ s}}$$

$$= 5.4 \times 10^3 \text{ m/s}$$

b) $m_s = ?$ $v = \sqrt{\frac{Gm_s}{r}} \Rightarrow m_s = \frac{v^2 r}{G}$

$$m_s = \frac{(5.4 \times 10^3)^2 (4.5 \times 10^{12} \text{ m})}{6.67 \times 10^{-11} \text{ Nm}^2/\text{kg}^2}$$

$$= 2.0 \times 10^{30} \text{ kg}$$

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7. $T = 29$ Earth years
 $= 915170400 \text{ s}$
 $v = 9.69 \text{ km/s}$
 $= 9.69 \times 10^3 \text{ m/s}$
 $r = ?$

$$v = \frac{d}{t} = \frac{2\pi r}{T}$$

$$r = \frac{vT}{2\pi}$$

$$= \frac{(9.69 \times 10^3 \text{ m/s})(915170400 \text{ s})}{2\pi}$$

$$= 1.4 \times 10^{12} \text{ m}$$

8. $r = 5.03 \times 10^{11} \text{ m}$

a) $v = ?$

$$m_s = 1.99 \times 10^{30} \text{ kg}$$

$$v = \sqrt{\frac{GM_s}{r}}$$

$$= \sqrt{\frac{(6.67 \times 10^{-11} \text{ N m}^2/\text{kg}^2)(1.99 \times 10^{30} \text{ kg})}{5.03 \times 10^{11} \text{ m}}}$$

$$= 1.62 \times 10^4 \text{ m/s}$$

b) $T = ?$

$$v = \frac{d}{t} = \frac{2\pi r}{T}$$

$$T = \frac{2\pi r}{v}$$

$$T = \frac{2\pi (5.03 \times 10^{11} \text{ m})}{1.62 \times 10^4 \text{ m/s}}$$

$$T = 195089025 \text{ s} \times \frac{1 \text{ h}}{3600 \text{ s}} \times \frac{1 \text{ d}}{24 \text{ h}} \times \frac{1 \text{ y}}{365.25 \text{ d}}$$

$$= 6.18 \text{ years}$$

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 $m = 1.99 \times 10^{30} \text{ kg}$
 $r = 4.05 \times 10^{12} \text{ m}$
 $v = ?$

$$v = \sqrt{\frac{Gm}{r}}$$

$$v = \sqrt{\frac{(6.67 \times 10^{-11} \text{ N m}^2/\text{kg}^2)(1.99 \times 10^{30} \text{ kg})}{4.05 \times 10^{12} \text{ m}}}$$

$$v = 5.43 \times 10^3 \text{ m/s}$$